

Research suggests that timed tests cause math anxiety *

JO BOALER, PROFESSOR OF MATHEMATICS EDUCATION, STANFORD UNIVERSITY

Teachers in the United States are often forced to follow directives that make little sense to them and are far removed from research evidence. One of the initiatives mandated by many school districts that I place high in the category of uninformed policy is the use of timed tests to assess math facts and fluency. Teachers and administrators use these

IN MY OPINION

tests with the very best of intentions, but they use them without knowledge of

the important evidence that is emerging from neuroscience. Evidence strongly suggests that timed tests cause the early onset of math anxiety for students across the achievement range. Given the extent of math anxiety, math failure, and innumeracy in the United States (Boaler 2009), such evidence is important for us all to consider. In this article, I summarize the evidence from neuroscience and describe an alternative pedagogical routine that teaches number sense and math fluency at the same time that it encourages mathematical understanding and excitement.

Math anxiety

Occurring in students from an early age, math anxiety and its effects are exacerbated over time, leading to



ALEXSTAR/THINKSTOCK

low achievement, math avoidance, and negative experiences of math throughout life (Ramirez et al. 2013; Young, Wu, and Menon 2012). Educators have witnessed the impact of math anxiety for decades, but only in recent years have timed math tests been shown to be one cause of the

early onset of math anxiety. Indeed, researchers now know that students experience stress on timed tests that they do not experience even when working on the same math questions in untimed conditions (Engle 2002).

In a recent study of 150 first and second graders, researchers measured students' levels of math anxiety, finding that children as young as first grade experienced it and that levels of math anxiety did not correlate with grade level, reading level, or parental income (Ramirez et al. 2013). Other researchers analyzed brain-imaging data from forty-six seven- to nine-year-old children while they worked on addition and subtraction problems and found that those students who "felt panicky" about math had increased activity in brain regions associated with fear. When those areas were active, decreased activity took place in the brain regions that are involved in problem solving (Young, Wu, and Menon 2012).

Beilock and her colleagues conducted brain scans to study the ways in which anxiety affects individuals, showing that children compute with math facts—such as those required in timed tests—by recalling information that is held in the working memory (Beilock 2011). The more working memory an individual

of math. Students also suffer from one of the most damaging myths that pervades U.S. math classrooms: the belief that *good* math performance is *fast* math performance. Award-winning mathematician Laurent Schwartz reflected in his 2001 autobiography that he often felt he was “unintelligent” when he was in school because he was one of the slower students:

At the end of the eleventh grade, I took the measure of the situation, and came to the conclusion that rapidity doesn't have a precise relation to intelligence. What is important is to deeply understand things and their relations to each other. This is where intelligence lies. The fact of being quick or slow isn't really relevant.

Unfortunately, many students across the United States come to believe that fast students are those who have the most potential, meaning that many slower but deep thinkers turn away from math. The hallmark of high-level mathematical thinking, as Schwartz reflects, is working in depth, not working at speed. Timed tests as well as other speed-related materials (such as flash cards) cause slow, strong mathematical thinkers to become discouraged in class, develop math anxiety, and turn away from the subject.

Encouraging number sense and automaticity

Some districts use timed tests because of words such as *automaticity* in the new Common Core State Standards for Mathematics (CCSSM) (CCSSI 2010). But much better methods of teaching automaticity exist that also help students develop the conceptual understanding of mathematics that they urgently need (Boaler 2009). *Number sense*—the ability to work flexibly with numbers, decomposing and regrouping them with confidence—is so critical to young children that it is known to separate high achievers from low

achievers in mathematics (Gray and Tall 1994, Boaler 2009). Pedagogical strategies called *number talks* (Parker 1993, Richardson 2011), also sometimes called *math talks*, help students develop math fluency and number sense at the same time. Importantly, they do so while showing students the flexibility and creativity within mathematics.

In a typical number talk, teachers give all students a number problem, such as $25 + 35$, $23 - 15$, or 18×5 . Problems can involve any number operations—addition, subtraction, multiplication, or division—and they can be posed at any level of difficulty. The problems chosen should be those that generate many different solution paths. After the teacher poses the problem, he or she asks students to think of ways to solve it in their heads and to show their thumb, privately, when they have a solution. The

reason for “quiet thumbs” rather than raised hands is to keep students from feeling intimidated or rushed when they see other students waving hands to show they have solved the problem. When the teacher sees the majority of thumbs up, she asks students to share their answers. If more than one student answers, teachers typically record the different answers without passing judgment on the “correctness” of the answers. Teachers then ask students to show how they have arrived at their answer. When I have taught middle school using number talks, students typically share six to eight different ways of arriving at the correct answer (see Boaler 2009). As students share their thinking, teachers record all their different methods next to one another on the board and ask students—by using such prompts as the following—to reflect on the different methods:

teaching
children
mathematics

Look Who's Talking...

Join your fellow readers
on TCM's new blog:

Math Tasks to Talk About

Ralph Connelly, a TCM panel member, shares his different perspective on the Handshake problem. Have you used it another way? Share with other TCM readers!

www.nctm.org/TCMblog/MathTasks

- Which ones are similar?
- Could we use the same method with different numbers?
- Would this method always work?

The visual representation of solutions is also helpful for students. In a recent online course I taught for teachers, I showed different visual representations of solutions for the expression 12×15 (see figs. 1–7). For the methods depicted in figures 4, 6, and 7, I asked students for visual representations of the solutions.

Different variants of number talks exist; some teachers ask students to indicate with their fingers if they have more than one method, for example. Number talks do not take long; they are short pedagogical routines (Kazemi, Lampert, and Ghouseini 2007) that take about ten minutes of lessons, but they achieve an incredible amount in that time. When I have used them with struggling seventh and eighth graders, students have reported that the number talks at the start of lessons completely changed their views of math. Many of them were incredulous to see an abstract number problem solved in eight different ways. They learned the critically important practice of number flexibility (Gray and Tall 1994), and they became more fluent with math facts. Number talks also work well with students of different achievement levels because students who know number facts well are usually fascinated to see and understand different methods, and students who

One teacher explained that she [gives weekly timed tests] because the first time she gave the test, many of her students cried; she now wants to get her students “used to them.”

are at an earlier stage of understanding also learn a great deal from the numerical solution paths. I have used the same problems with struggling seventh graders, Stanford freshmen, and CEOs of successful businesses with equally high engagement. Parrish (2010), Harris (2001), and Boaler (2009) give different examples of number talks.

CCSSM (CCSSI 2010) asks that students develop *automaticity* and that they know math facts by heart. Students can practice math facts in many ways, without the pressure of speed, including the use of hundred charts and many of the games and apps that have emerged in recent years. Number talks play an important part in the development of fluency: Students who answer mental number problems on a daily basis quickly commit the math facts they use to heart, at the same time developing something much more important—number sense.

One reason that teachers give timed tests is to encourage students to work quickly with math, to help them achieve highly on math tests. But giving students

Seven representative solutions for the expression 12×15

FIGURE 1

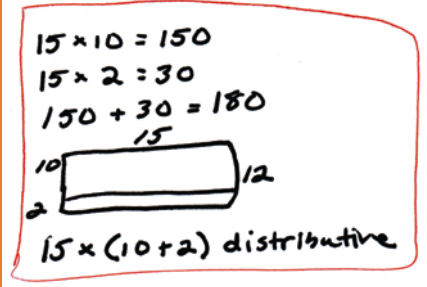


FIGURE 2

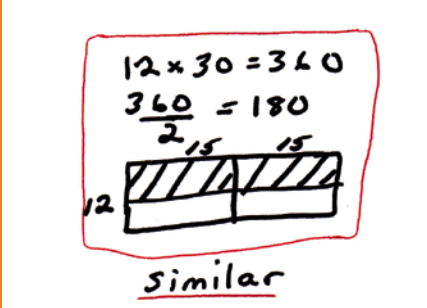


FIGURE 3

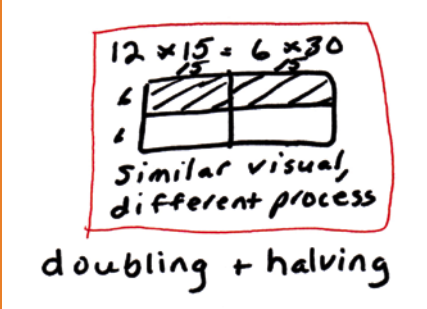
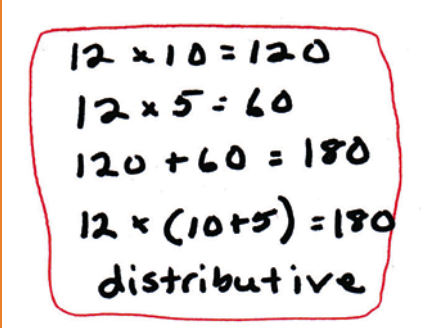


FIGURE 4



In our sister journals*

mathematics
teaching in the MIDDLE SCHOOL



The Cartoon Corner department in the April issue of *MTMS* features “Play Ball!” by David B. Spangler and A. Katie Hendrickson, an exploration of odds and probabilities related to baseball. A full-page activity sheet is included.

“Out of the Park: Using the Mean in Sports” appears in the March *SEM*, an online resource for grades 5–10 students, teachers, and teacher educators. Means are often used to compare athletes’ performances in sports. Points per game, batting averages, strikeouts per game, earned run averages, blocked shots per game, and many other means can have an impact amounting to millions of dollars on some athletes, whose contracts may be negotiated on the basis of their batting average, earned run average, passing rating, or points scored per game. Means are also a way to think about investing money for one’s future. *SEM* is one of the many benefits of NCTM membership. Access *SEM* at <http://www.nctm.org/publications/default.aspx>.

FIGURE 5

$$12 \times 12 = 144$$

$$12 \times 3 = 36$$

$$12 \times (12 + 3)$$

distributive

FIGURE 6

$$12 \times 15$$

$$12 \times 15 = (3 \times 4) \times 15$$

$$= 3 \times (4 \times 15)$$

$$= 3 \times 60$$

$$= 180$$

associative

FIGURE 7

$$12 \times 15 = 12 \times (5 \times 3)$$

$$= (12 \times 5) \times 3$$

$$= 60 \times 3$$

associative

timed tests often achieves the opposite of this goal—creating math anxiety and a fear of mathematics that hinders future test performance. When taking timed tests, children who are fast usually remain fast while children who are slow remain slow—and become slower as math anxiety sets in. Teaching students to develop fluency and work at a reasonable pace is something that is achieved through the careful development of numerical understanding in the early years of school. Learning is a process that takes time, and it cannot be accelerated by methods that encourage speed at the expense of understanding.

The best mathematical learning environments are those in which students are encouraged to appreciate the beauty and diversity of math, learning new ideas without pressure or anxiety. Many students turn away from math in their early years because they feel that their creativity and open thinking close down as they are forced to follow standard rules and procedures. Mathematics is a multidimensional subject that should be introduced in the early years through a flexible, visual, and creative approach that values students’ thinking at all times (Boaler 2009). Number talks achieve these goals while teaching students numerical flexibility and automaticity. All educators want students to succeed in math and develop a love of math, but policies that require testing young children under timed conditions may be inadvertently achieving the opposite.

BIBLIOGRAPHY

- Ashcraft, Mark H. 2002. “Math Anxiety: Personal, Educational and Cognitive Consequences.” *Current Directions in Psychological Science* 11 (5): 181–85.
- Beilock, Sian L. 2011. *Choke: What the Secrets of the Brain Reveal about Getting It Right When You Have To*. New York: Simon and Schuster, Free Press.
- Beilock, Sian L., Elizabeth A. Gunderson, Gerardo Ramirez, and Susan C. Levine. 2009. “Female Teachers’ Math Anxiety Affects Girls’ Math Achievement.” *Proceedings of the National Academy of Sciences* 107 (5): 1860–63. doi:10.1073/pnas.0910967107
- Boaler, Jo. 2009. *What’s Math Got to Do with It? Helping Children Learn to Love Their Least Favorite Subject—and Why It’s Important for America*. New York: Penguin.
- . 2013. “Ability and Mathematics: The Mindset Revolution That Is Reshaping Education.” *FORUM* 55 (1): 143–52.
- Common Core State Standards Initiative (CCSSI). 2010. *Common Core State Standards for Mathematics*. Washington, DC: National Governors Association Center for Best Practices and the Council of Chief State School Officers. http://www.corestandards.org/assets/CCSSI_Math%20Standards.pdf
- Engle, Randall W. 2002. “Working Memory Capacity as Executive Attention.” *Current Directions in Psychological Science* 11:19–23.
- Faust, Michael W. 1992. *Analysis*



- of *Physiological Reactivity in Mathematics Anxiety*. Ph.D. diss., Bowling Green State University, Ohio.
- Gray, Eddie M., and David O. Tall. 1994. "Duality, Ambiguity, and Flexibility: A 'Proceptual' View of Simple Arithmetic." *Journal for Research in Mathematics Education* 25 (March): 116–40.
- Harris, Pamela W. 2001. *Building (Powerful) Numeracy for Middle and High School Students*. Portsmouth, NH: Heinemann.
- Hembree, Ray. 1990. "The Nature, Effects, and Relief of Mathematics Anxiety." *Journal for Research in Mathematics Education* 21 (January): 33–46.
- Kazemi, Elham, Magdalene Lampert, and Hala Ghouseini. 2007. *Conceptualizing and Using Routines of Practice in Mathematics Teaching to Advance Professional Education*. Report to the Spencer Foundation. Ann Arbor, MI.
- Lambert, R. 2013. Pers. Communication.
- Parker, Ruth. 1993. *Mathematical Power: Lessons from a Classroom*. Portsmouth, NH: Heinemann.
- Parrish, Sherry. 2010. *Number Talks, Grades K–5: Helping Children Build Mental Math and Computation Strategies*. Sausalito, CA: Math Solutions Publications.
- Ramirez, Gerardo, Elizabeth A. Gunderson, Susan C. Levine, and Sian L. Beilock. 2013. "Math Anxiety, Working Memory and Math Achievement in Early Elementary School." *Journal of Cognition and Development* 14 (2): 187–202.
- Richardson, Frank C., and Robert L. Woolfolk. 1980. "Mathematics Anxiety." In *Test Anxiety: Theory, Research, and Application*, edited by Irwin G. Sarason, pp. 271–88. Hillsdale, NJ: Lawrence Erlbaum Associates.
- Richardson, Kathy. 2011. "What Is the Distinction between a Lesson and a Number Talk?" http://mathperspectives.com/pdf_docs/mp_lesson_ntalks_distinction.pdf

A critical Common Core tool: Progressions documents

BY ROBYN SILBEY, PD AND CAMPUS CONSULTANT

The Progressions documents, funded by the Brookhill Foundation, preceded the Common Core State Standards in Mathematics (CCSSM) (CCSSI 2010) and provided its foundation. The Progressions describe the conceptual development of a topic strand across several grade levels. Once completed, each strand was sliced into grade-level standards, on the basis of the logical structure and sequence of mathematics and children's cognitive development.

The Progressions documents explain why standards are sequenced the way they are, call attention to areas in which misunderstandings are common, and offer suggestions and pedagogical solutions. They provide a critical tool (a) as a mechanism between mathematics education research and the standards, (b) to assist in long-range, unit, weekly, and daily planning, and (c) for math leaders and coaches to share with classroom teachers. Each Progressions document contains the following:

- An overview
- A detailed discussion of the work in each grade level
- Connections to the Standards for Mathematical Practice
- Concrete examples that may be used for instruction

The Progressions documents should be considered by every district, school, and teacher as one of the most useful tools for professional development and curriculum design. The documents can be found at <http://ime.math.arizona.edu/progressions/>. On the home page, simply click on a link that describes the progression of any content strand and grade-level band, such as the Draft K–6 Progression on Geometry, the Draft K–5 Progression on Number and Operations in Base Ten, or the Draft Grades 3–5 Progression on Number and Operations–Fractions. You can also find additional information about the Progressions project and its brilliant working team.

Direct questions and comments about this article to rsilbey@hotmail.com.

- Schwartz, Laurent. 2001. *A Mathematician Grappling with His Century*. Bern: Birkhäuser Basel.
- Seeley, Cathy. 2009. *Faster Isn't Smarter*. Sausalito, CA: Math Solutions Publications.
- Young, C. B., Sarah Wu, and Vinod Menon. 2012. "The Neurodevelopmental Basis of Math Anxiety." *Psychological Science Online First*. March 20, 2012. doi:10.1177/0956797611429134



Jo Boaler, www.joboaler.com, is a Professor of Mathematics Education at Stanford University and founder of youcubed, a website to give teachers and parents resources and ideas to inspire and excite students about math. Among many other accomplishments, she is the editor for the Research Commentary Section of *The Journal for Research in Mathematics Education (JRME)*, an analyst for PISA testing in the OECD, and author of the first MOOC on mathematics teaching and learning.